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LETTER TO THE EDITOR

Magnetic correlations and spin dynamics in the t-t'-J model

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Abstract. Using a generalized RPA expression for the spin susceptibility, we investigate the spin dynamical properties in the normal state of the metallic cuprates on the basis of a spin-rotation-invariant slave boson representation of the t-t'-J model, where the second-neighbour hopping t' incorporates important correlation and band structure effects near half-filling. We attribute the contrasting q dependence of the magnetic structure factor $S(q, \omega)$ seen in neutron scattering experiments for LSCO- and YBCO-type systems to differences in their Fermiology. Assuming that the antiferromagnetic correlations are spatially filtered by the hyperfine form factors, we calculate the temperature dependences of spin-lattice and spin-spin relaxation rates for planar copper and oxygen sites: the results agree qualitatively well with various experiments on YBa₂Cu₃O_{6+x}.

The low-energy physics of the high- T_c cuprates is determined by the charge and spin dynamics in the CuO_2 layers. In particular, the nature of spin excitations has been extensively studied by means of nuclear magnetic/quadrupole resonance (NMR/NQR) and inelastic neutron scattering (INS) techniques clarifying the persistence of strong antiferromagnetic (AF) correlations in the normal and superconducting states [1, 2]. Detailed investigations of the wavevector dependence of the low-frequency spin fluctuation spectrum have revealed remarkable differences between the YBa₂Cu₃O_{6+x} (YBCO) and La_{2-x}Sr_xCuO₄ (LSCO) families at low doping level x; the dynamic structure factor $S(q, \omega)$ keeps its maximum at (π, π) in the YBCO system, while in LSCO, the peaks are displaced from the commensurate position to the four incommensurate wave vectors $(\pi \pm q_0, \pi), (\pi, \pi \pm q_0),$ where $q_0 \sim 2\pi x$. On the other hand, the analysis of the NMR data shows that the relaxation rates on the planar Cu sites are similar in all materials. Two striking features are associated with ${}^{63}T_1^{-1}$: (i) as a result of strong local spin fluctuations on 63 Cu sites, it is enhanced by an order of magnitude over the oxygen rate ${}^{17}T_1^{-1}$; and (ii) in sharp contrast to the Korringa-like behaviour at the planar ¹⁷O sites, its temperature dependence does not follow the Korringa law. Several scenarios have been proposed to analyse theoretically the neutron and nuclear relaxation data in the cuprates ranging from weak- [3, 4] and strong-coupling [5] Fermiliquid based, phenomenological nearly AF [6, 7] and marginal Fermi-liquid schemes [8] to mean-field gauge theory approaches to the t-J model [9].

In the present letter, we try to understand the INS and NMR experiments on the basis of a slave boson mean field theory of the t-t'-J model using simple approximations for the spin susceptibility and various q-dependent hyperfine form factors.

The Hamiltonian describing the t-t'-J model is

$$\mathcal{H}_{t-t'-J} = -t \sum_{\langle i,j \rangle,\sigma} \tilde{c}_{i\sigma}^{\dagger} \tilde{c}_{j\sigma} - t' \sum_{\langle \langle i,j \rangle \rangle,\sigma} \tilde{c}_{i\sigma}^{\dagger} \tilde{c}_{j\sigma} + J \sum_{\langle ij \rangle} \left(\boldsymbol{S}_{i} \cdot \boldsymbol{S}_{j} - \frac{n_{i}n_{j}}{4} \right).$$
(1)

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The effective one-band model (1) incorporates both strong correlation and band structure effects. Apart from the usual nearest-neighbour (NN) transfer t, $\mathcal{H}_{t-t'-J}$ includes direct next-NN hopping processes t' on a square lattice. From band structure theory, a ratio t'/t = -0.4 (0 to -0.16) has been found for the YBCO (LSCO) family, where t = 0.3-0.4 eV. Note that the t' term suffices to reproduce the different Fermi surface geometries of YBCO and LSCO. Moreover, the inclusion of t' coupling the same sublattice becomes crucial for the low-lying magnetic excitations. In (1), J measures the AF exchange interaction.

To treat the strong electronic correlations, we adopt the $SU(2) \otimes U(1)$ spin-rotationinvariant slave boson (SRI SB) technique [10], which differs from the spinon-holon schemes [9, 11], for the t-t'-J Hamiltonian. Within an SB functional integral representation of (1), the electronic operators acting in a projected Hilbert space without double occupancy are mapped onto the products

$$\tilde{c}_{i\sigma} \to \sum_{\rho} z_{i\sigma\rho} f_{i\rho} \tag{2}$$

of a fermion (anticommuting) $f_{i\rho}$ and a boson (commuting) \mathbf{z}_i field operators. The hopping operators $\mathbf{z}_i^{(\dagger)} = \mathbf{z}_i^{(\dagger)}(e_i, e_i^{\dagger}, \mathbf{p}_i, \mathbf{p}_i^{\dagger})$ yield a correlation-induced band renormalization. Here (scalar) $e_i^{(\dagger)}$ and (matrix) $\mathbf{p}_i^{(\dagger)}$ SB operators refer to empty and single-occupied states at site *i*. The (pseudo-) fermions $f_{i\rho}^{\dagger}$ are components of a spinor field $\Psi_i^{\dagger} = (f_{l\alpha}^{\dagger}, f_{l\beta}^{\dagger})$ and hence SRI is ensured. The interaction term is bosonized via

$$n_i \rightarrow 2 \operatorname{Tr} \mathbf{p}_i^{\dagger} \mathbf{p}_i$$
 (3)

$$S_i \to \operatorname{Tr} \mathbf{p}_i^{\dagger} \tau \mathbf{p}_i.$$
 (4)

Unphysical states in the extended (bosonic and fermionic) Fock space are eliminated by imposing a set of local constraints:

$$e_i^{\dagger} e_i + 2 \operatorname{Tr} \mathbf{p}_i^{\dagger} \mathbf{p}_i = 1$$
 completeness (5)

$$\Psi_i \otimes \Psi_i^{\dagger} + 2\mathbf{p}_i^{\dagger} \mathbf{p}_i = \tau_o \qquad (1 - 1 - \text{correspondence}). \tag{6}$$

Using the SRI SB functional integral theory at the saddle point level, we have studied [12] the *static* magnetic properties of the 2D t-t'-J model, in particular the ground-state phase diagram, including incommensurate magnetic structures and phase-separated states. Furthermore we have calculated the doping dependence of the Hall resistivity, the results being in accord with experiments on La_{2-x}Sr_xCuO₄, YBa₂Cu₃O_{6+x} and Nd_{2-x}Ce_xCuO₄ [13]. In this letter, we focus on the spin *dynamical* properties in the *paraphase* of the extended t-J model (1), where we will use an RPA-like form for the exchange-enhanced spin susceptibility [9, 11, 14]

$$\chi_s(q,\omega) = \frac{\overline{\chi}_o(q,\omega)}{1 + (J/2)(\cos q_x + \cos q_y)\overline{\chi}_o(q,\omega)}.$$
(7)

The irreducible susceptibility $\overline{\chi}_o(q, i\omega_m) = -(2/\beta N) \sum_{k,n} \overline{G}(k, i\omega_n) \overline{G}(k+q, i\omega_{n+m})$ contains the (dressed) SB Green propagators $\overline{G}(k, i\omega_n) = [i\omega_n - E_k + \tilde{\mu}]^{-1}$ describing non-interacting electrons with a *renormalized* band structure

$$E_{k} = -2z^{2}t \left[\cos k_{x} + \cos k_{y} + 2(t'/t) \cos k_{x} \cos k_{y}\right].$$
(8)

The (shifted) chemical potential $\tilde{\mu}$ is fixed by the requirement $n = (2/N) \sum_{k} [\exp(\beta (E_k - \tilde{\mu})) + 1]^{-1}$, where $\beta = 1/k_{\rm B}T$. Note that the band renormalization factor $z^2 = 2\delta/(1+\delta)$ varies strongly with hole concentration $\delta = 1 - n$.

Once the dynamic spin susceptibility has been obtained, both INS measurements and NMR/NQR experiments can be explored. From the fluctuation-dissipation theorem the q-and ω -dependent spin structure factor

$$S(q,\omega) = \frac{1}{\pi} \frac{1}{1 - \exp(-\beta\hbar\omega)} \operatorname{Im} \chi_s(q,\omega)$$
(9)

probed by INS is related to the dynamical susceptibility. On the other hand, the nuclear spin-lattice relaxation rate ${}^{a}T_{1\alpha}^{-1}$ ($\alpha = \bot$, \parallel), e.g. for a field H_{α} applied parallel to the c axis, given by [6]

$$\left({}^{a}T_{1\parallel}T\right)^{-1} = \frac{1}{2}\frac{k_{\rm B}}{\mu_{B}^{2}\hbar}\lim_{\omega\to 0}\frac{1}{N}\sum_{q}^{a}F_{\perp}^{2}(q)\frac{{\rm Im}\,\chi_{s}(q,\omega)}{\hbar\omega}$$
(10)

and transverse spin-spin relaxation rate, T_{2G}^{-1} , for the RKKY coupling of the nuclear Cu spins given by [15]

$$T_{2G}^{-2} = \frac{c}{8\hbar^2} \frac{1}{(2\mu_B)^4} \left\{ \frac{1}{N} \sum_{q} \left(F_{\parallel}^2(q) \chi_s(q) \right)^2 - \left(\frac{1}{N} \sum_{q} F_{\parallel}^2(q) \chi_s(q) \right)^2 \right\}$$
(11)

provide local, atomic-site- ($a = \{63, 17\}$ -) specific information. Here μ_B denotes the Bohr magneton and the constant c = 0.69 is the natural abundance fraction of the ⁶³Cu isotope. The form factors are given for ⁶³Cu and the planar ¹⁷O nucleus as [16]

$$^{63}F_{\alpha}(q) = A_{\alpha} + 2B(\cos q_x + \cos q_y) \tag{12}$$

$${}^{17}F_{\alpha}(q) = 2C\cos(q_x/2).$$
 (13)

Together with the anisotropy of the Cu relaxation rates, the measurements of the Knight shift

$${}^{a}K_{\alpha} = \frac{1}{2} \frac{1}{\mu_{\rm B}^{a} \gamma_{n} \hbar} \lim_{q \to 0} {}^{a}F_{\alpha}(q) \chi_{s}(q, \omega = 0)$$
⁽¹⁴⁾

have been used to determine the hyperfine coupling constants A_{α} , B and C on the basis of the Mila-Rice Hamiltonian [17]. Following [6] we take $A_{\parallel} \approx -4B$, $A_{\perp} \approx 0.84B$, $C \approx 0.87B$ and $B \approx 3.3 \times 10^{-7}$ eV, where ${}^{63}\gamma\hbar = 7.5 \times 10^{-24}$ erg G⁻¹ and ${}^{17}\gamma\hbar = 3.8 \times 10^{-24}$ erg G⁻¹.

In order to make contact with the experimental situation in the cuprates, in the numerical work we fix J/t = 0.4, and take t = 0.3 eV as the energy unit. As we know, the RPA susceptibility contains an unphysical instability of the paramagnetic phase at some particular wave vector q below a critical doping δ_c as signalled by the zero in the denominator of (7) at $\omega = 0$ (Stoner condition). Therefore the use of (7) only makes sense if the system is far from the magnetic instability, i.e., $\delta > \delta_c$, where for J = 0.4 we have $\delta_c(t'/t = -0.16) \simeq 0.27$ and $\delta_c(-0.4) \simeq \delta_c(0) \simeq 0.17$.

We begin with a discussion of the RPA dynamical spin structure factor $S(q, \omega)$. The q dependence of $S(q, \omega)$ along the main symmetry axis of the Brillouin zone is shown in figure 1 for different ratios t'/t, J = 0.4 and hole density $\delta = 0.3$. Here the temperature is T = 35 K and the frequency $\hbar \omega = 10$ meV. For LSCO-type parameters (t'/t = 0, -0.16) we found four pronounced incommensurate peaks located at the points $(\pi \pm q_0, \pi), (\pi, \pi \pm q_0)$. The incommensurate modulation wave vectors move with increasing doping level δ away from the corner of the Brillouin zone along the directions $(1, \pi)$ or $(\pi, 1)$ (square lattice notation). Note that while the incommensurate peak position obtained from a three-band RPA calculation of $S(q, \omega)$ [5] can be parametrized consistent with the experimental observation that $q_0 \simeq 2\pi x$ [18], all the effective one-band RPA approaches [9, 19] yield



Figure 1. Dynamic magnetic structure factor $S(q, \omega)$ plotted along the (1,1) and (1, π) directions of the Brillouin zone for different ratios t'/t.



Figure 2. Spin-lattice relaxation rates ${}^{63}T_{1\parallel}^{-1}$ and ${}^{17}T_{1\parallel}^{-1}$ (inset) as a function of temperature. SB results (+; t'/t = -0.4, $\delta = 0.35$) are compared with experiments (Δ) on YBa₂Cu₃O₇ [23].

an incommensurability scaling rather as $q_0 \simeq \pi \delta$ (in the LSCO systems the concentration of the chemically doped charge carriers in the CuO₂ planes (δ) definitely agrees with the composition (x) of the substituent Sr). A more detailed investigation of the LSCO-type qscans show that the q variation of $S(q, \omega)$ is mainly governed by that of $\overline{\chi}_0(q, \omega)$ and, in accordance with experiments [20], the incommensurate peaks considerably broaden as temperature or energy transfer are increased [21]. By contrast, the same plot for YBCOtype (t'/t = -0.4) parameters shows a broad, nearly *T*-independent [21], maximum around the (π, π) point [22] (see figure 1) which, due to the flat topology of $\overline{\chi}_0$, mainly reflects the q dependence of J(q) (cf. (7)). In this way, our calculations confirm recent arguments [5, 8, 9] for the importance of band structure (Fermi-surface geometry) effects in explaining the difference between observed LSCO and YBCO spin dynamics. Nevertheless, the question whether the incommensurate signals arise from an intrinsic magnetic structure or whether they result from the formation of domains (charge superstructures) in the LSCO system remains unanswered by INS [2, 16].

In a next step, we calculate the longitudinal or spin-lattice relaxation rate, T_1^{-1} , using the hyperfine form factors (12) and (13). In figure 2 the temperature dependences of ${}^{63}T_{1\parallel}^{-1}$ and $^{17}T_{10}^{-1}$ (inset) are shown for $\delta = 0.35$ and t'/t = -0.4 in comparison with experiments [23] on fully oxygenated YBCO materials (x = 1). Although our theory does not succeed in giving the correct amplitude of ${}^{a}T_{10}^{-1}$ the qualitative features of the NMR data are described surprisingly well. Obviously the broad magnetic peak in $S(q, \omega)$ at the AF wave vector $Q_{AF} = (\pi, \pi)$ strongly enhances the relaxation rate on Cu sites while, due to a geometrical cancellation $({}^{17}F_{\alpha}(q \simeq Q_{\rm AF}) \simeq 0)$, the corresponding oxygen rate is rather insensitive to nearly commensurate AF fluctuations, and therefore is governed by the long-wavelength part $q \simeq 0$ of the spin susceptibility [2]. For ⁶³Cu, the nominal Korringa ratio $S \equiv (1/T_1 T K_S^2)$ $(K_{\rm S}$ denotes the spin part of the Knight shift) is at least one order of magnitude larger. As can be seen from figure 2, for YBa₂Cu₃O₇-type parameters, a Korringa $(1/T_1 \propto T)$ dependence (dotted line) holds at both Cu and O sites below $T^* \sim 120$ K, demonstrating the existence of a characteristic temperature T^* as in all other near-optimum- T_c compounds [2, 24]. T^* is in good agreement with the coherence energy scale suggested experimentally [24]. Above T^* , the ¹⁷O NMR relaxation remains linear whereas the ⁶³Cu relaxation time does not follow the Korringa law. Similar results are found for the LSCO system [21].



Figure 3. ⁶³Cu and planar ¹⁷O relaxation data (\Diamond) for underdoped YBa₂Cu₃O_{6.6} [25] are plotted against temperature. Theoretical results (\times) are given at t'/t = -0.4 and $\delta = 0.2$.

In the oxygen-deficient compound YBa₂Cu₃O_{6.6}, $1/({}^{63}T_{1\parallel}T)$ shows a broad maximum at about 150 K (see figure 3), which reflects a strong deviation from the canonical Korringa behaviour. In the normal state regime the theoretical results agree even quantitatively with the experimental 63 Cu NMR data [25]. At this point it is important to stress that the present theory incorporates considerable band renormalization effects already via $\overline{\chi}(q, \omega)$, especially



Figure 4. $T_{2G}/(^{63}T_{1\parallel}T)$ in underdoped YBa₂Cu₃O_{6.6} (δ) as measured by Takigawa [15] compared with the SB data (x) at t'/t = -0.4 and $\delta = 0.2$.

at low doping level. Thus a rather moderate strength J = 0.4 of the AF exchange interaction yields the experimentally observed enhancement of ${}^{63}T_{1\parallel}^{-1}$. In striking contrast to the optimally doped YBCO system, the Korringa relation is no longer satisfied for the planar ¹⁷O nucleus sites in the underdoped material (cf. inset figure 3). Instead, a different behaviour ${}^{17}T_{1\parallel}T^{17}K_s$ = constant was suggested to hold down to T_c [25]. The unconventional Tscaling of ${}^{17}T_{1\parallel}$ has been taken as a signature for another important feature of the normal state spin dynamics, the so-called spin gap behaviour [2].

Complementary measurements of the transverse spin-spin relaxation rate, T_{2G}^{-1} , have provided further insights into the drastic change in the magnetic properties when passing from the overdoped to the underdoped regime [15, 26]. As experimentally observed, we found that T_{2G}^{-1} increases (decreases) with increasing (decreasing) hole doping (temperature) [21]. In order to detect the opening of a spin pseudogap as a function of T, a powerful technique is to measure the ratio T_{2G}/T_1T [27] which is nearly constant above ~ 200 K for deoxygenated YBa₂Cu₃O_{6.6} [15]. The calculated temperature dependence of this quantity is shown in figure 4 together with recent experimental results [15]. Most noticably, the opening of a spin pseudogap at $T^* \simeq 135$ K [27], i.e. well above T_c , is clearly seen as a decrease of T_{2G}/T_1T below T^* . Note that for YBa₂Cu₃O₇, as predicted by Fermi liquid theories, the ratio T_{2G}^2/T_1T is approximately constant above ~ 150 K [2].

In conclusion, we have shown that our SB treatment of the spin dynamics in high- T_c compounds, which incorporates important strong correlation and band structure (Fermi surface) effects in terms of the t-t'-J model, provides a reasonable explanation of the basic features of both INS and NMR experiments on LSCO and YBCO systems.

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